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EXAMINER

ROSARIO-VASQUEZ, DENNIS

ART UNIT	PAPER NUMBER
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2621

DATE MAILED: 11/12/2004

Please find below and/or attached an Office communication concerning this application or proceeding.

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<b>Office Action Summary</b>	<b>Application No.</b>		<b>Applicant(s)</b>	
	10/032,394		PRAKASH ET AL.	
	<b>Examiner</b>		<b>Art Unit</b>	
	Dennis Rosario-Vasquez		2621	

**-- The MAILING DATE of this communication appears on the cover sheet with the correspondence address --**  
**Period for Reply**

A SHORTENED STATUTORY PERIOD FOR REPLY IS SET TO EXPIRE 3 MONTH(S) FROM THE MAILING DATE OF THIS COMMUNICATION.

- Extensions of time may be available under the provisions of 37 CFR 1.136(a). In no event, however, may a reply be timely filed after SIX (6) MONTHS from the mailing date of this communication.
  - If the period for reply specified above is less than thirty (30) days, a reply within the statutory minimum of thirty (30) days will be considered timely.
  - If NO period for reply is specified above, the maximum statutory period will apply and will expire SIX (6) MONTHS from the mailing date of this communication.
  - Failure to reply within the set or extended period for reply will, by statute, cause the application to become ABANDONED (35 U.S.C. § 133).
- Any reply received by the Office later than three months after the mailing date of this communication, even if timely filed, may reduce any earned patent term adjustment. See 37 CFR 1.704(b).

#### Status

- 1) ☒ Responsive to communication(s) filed on 19 December 2001.
- 2a) ☐ This action is **FINAL**.                      2b) ☒ This action is non-final.
- 3) ☐ Since this application is in condition for allowance except for formal matters, prosecution as to the merits is closed in accordance with the practice under *Ex parte Quayle*, 1935 C.D. 11, 453 O.G. 213.

#### Disposition of Claims

- 4) ☒ Claim(s) 1-42 is/are pending in the application.
- 4a) Of the above claim(s) \_\_\_\_\_ is/are withdrawn from consideration.
- 5) ☐ Claim(s) \_\_\_\_\_ is/are allowed.
- 6) ☒ Claim(s) 1-42 is/are rejected.
- 7) ☐ Claim(s) \_\_\_\_\_ is/are objected to.
- 8) ☐ Claim(s) \_\_\_\_\_ are subject to restriction and/or election requirement.

#### Application Papers

- 9) ☒ The specification is objected to by the Examiner.
- 10) ☒ The drawing(s) filed on 19 December 2001 is/are: a) ☒ accepted or b) ☐ objected to by the Examiner.  
Applicant may not request that any objection to the drawing(s) be held in abeyance. See 37 CFR 1.85(a).  
Replacement drawing sheet(s) including the correction is required if the drawing(s) is objected to. See 37 CFR 1.121(d).
- 11) ☐ The oath or declaration is objected to by the Examiner. Note the attached Office Action or form PTO-152.

#### Priority under 35 U.S.C. § 119

- 12) ☐ Acknowledgment is made of a claim for foreign priority under 35 U.S.C. § 119(a)-(d) or (f).
- a) ☐ All    b) ☐ Some \* c) ☐ None of:
1. ☐ Certified copies of the priority documents have been received.
  2. ☐ Certified copies of the priority documents have been received in Application No. \_\_\_\_\_.
  3. ☐ Copies of the certified copies of the priority documents have been received in this National Stage application from the International Bureau (PCT Rule 17.2(a)).
- \* See the attached detailed Office action for a list of the certified copies not received.

#### Attachment(s)

- |  |   |
|--|---|
| 1) <input checked="" type="checkbox"/> Notice of References Cited (PTO-892)  | 4) <input type="checkbox"/> Interview Summary (PTO-413)<br>Paper No(s)/Mail Date. _____ |
| 2) <input type="checkbox"/> Notice of Draftsperson's Patent Drawing Review (PTO-948)   | 5) <input type="checkbox"/> Notice of Informal Patent Application (PTO-152)             |
| 3) <input checked="" type="checkbox"/> Information Disclosure Statement(s) (PTO-1449 or PTO/SB/08)<br>Paper No(s)/Mail Date <u>5/23/02</u> | 6) <input type="checkbox"/> Other: _____  |

## **DETAILED ACTION**

### ***Priority***

1. Applicant's claim for domestic priority under 35 U.S.C. 119(e) is acknowledged.

### ***Information Disclosure Statement***

2. The IDS filed on May 28, 2002 has three references on page 2, last three that were not considered because they were present. Please submit the last three references.

### ***Specification***

3. The disclosure is objected to because of the following informalities:

Page 7, line 11: "must transmitted" ought to be amended to "must be transmitted".

Page 15, line 22: "Fig 9A-C" ought to be amended to "Fig. 9A-B".

Page 16, line 22: "in sections A-C" is unfounded. A suggestion is to label each corresponding section in the previous pages with A-C.

Page 18, line 4: "arbitrarily" ought to be amended to "arbitrary".

Page 18, line 22: "assumed to well" ought to be amended to "assumed to be well".

Page 23, line 10: "can coupled" ought to be amended to "can be coupled".

Page 24, line 10: "14B, the result in Fig. 14C" ought to be amended to "14A, the result in Fig. 14B".

Page 29, line 11 "based one" ought to be amended to "based on one".

Page 26, line 16 has two periods.

Page 30, last line: "we an example" ought to be amended to "an example"

Page 31, line 3: "will interpolated" ought to be amended to "will be interpolated".

Page 31, line 18: "thos weights" ought to be amended to "those weights".

Appropriate correction is required.

### ***Claim Objections***

4. The following quotations of 37 CFR § 1.75(a) is the basis of objection:

(a) The specification must conclude with a claim particularly pointing out and distinctly claiming the subject matter which the applicant regards as his invention or discovery.

5. Claims 1,2,4,5,9,10,18,19,21,23,25,27,28,32,33,34,37 are objected to under 37 CFR § 1.75(a) as failing to particularly point out and distinctly claim the subject matter which the applicant regards as his invention or discovery.

6. The disclosure is objected to because of the following informalities:

Claims 1,2,5 and 33 are missing periods.

Claim 4, line 7 has a misplaced period that ought to be deleted.

Claims 9 and 10 has the phrase "5, or 6" which are claims that have no antecedent basis for transmitting of claim 9 or quantizing of claim 10.

Claim 18, lines 2,3 has the phrase "the forward transform" which has no antecedent basis and ought to be amend to "a forward transform".

Claim 19, line 2,3 has the phrase "the inverse transform" which has no antecedent basis.

Claim 21, line 2 has the phrase "the pattern adaptive transform" has no antecedent basis.

Claim 23, line 3: "the reconstruction phase" has no antecedent basis.

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Claims 25 and 26, lines 3,4 "the filter", "the mathematical result" and "the convolution" have no antecedent basis.

Claim 27, lines 2,3:"the result", "the transition", and "the boundary" have no antecedent basis.

Claim 28, lines 2,3:"the pixel value differences" have no antecedent basis. A suggestion is to amend "the pixel value differences" to "a plurality of pixel value differences".

Claim 32, line 2:"the data values" has no antecedent basis. A suggestion is to amend "the data values" to "the weighted average".

Claim 34, lines 2-5:"the transition", "the decoder", "the operation" and "the inverse transform" have no antecedent basis.

Claim 37, lines 1 and 3:"the needed function" and "the remaining pixels values" have no antecedent basis.

Appropriate correction is required.

***Claim Rejections - 35 USC § 102***

7. The following is a quotation of the appropriate paragraphs of 35 U.S.C. 102 that form the basis for the rejections under this section made in this Office action:

A person shall be entitled to a patent unless –

(b) the invention was patented or described in a printed publication in this or a foreign country or in public use or on sale in this country, more than one year prior to the date of application for patent in the United States.

8. Claims 1-42 are rejected under 35 U.S.C. 102(b) as being anticipated by Yamaguchi et al. (US Patent 5,978,514 A).

Regarding claim 4, Yamaguchi et al. discloses a method of processing all or a portion of a multi-dimensional signal with a domain (A signal S1 of figure 1 has a domain of 16 X 16 pixels in col. 14, lines 59-61.) composed of a collection of arbitrarily shaped domains (Fig. 5(a) shows a rectangular ring 31.) via a multi-scale transform (fig. 2,num. 17:DCT contained in fig. 1,num. 10:CODING MEANS) comprising the steps of:

a. Obtaining a multi-dimensional digital image frame (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num.

3:SCREEN-AREA DETERMINING MEANS.)

b. Breaking the image frame into constituent arbitrary shaped domains, or given such a set (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num. 3:SCREEN-AREA DETERMINING MEANS and contain an "optional shape" in col. 13, line 61. ), that cover all or a portion (The signal S1 has "micoblocks composed of 16 X 16 pixels (col. 14, lines 59-61)".) of the original multi-dimensional signal domain (Signal S1 of figure 1 has a domain of 16 X 16 pixels in col. 14, lines 59-61 that corresponds to the block.).

c. Performing the domain adaptive (Fig. 2,num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2,num. 17:DCT contained in fig. 1,num. 10:CODING MEANS)

d. Quantizing (fig. 2, num. 21 : QUANTIZATION CIRCUIT) [the] **a plurality** of resultant decomposition coefficients (FIG. 2, um. 17 outputs coefficients to fig. 2, num. 21:QUANTIZATION CIRCUIT.)

e. Encoding (Fig. 2, num. 13:MODE DETERMINING MEANS provides for two types of encoding in col. 15, lines 1-5.) and transmitting the quantized values (Fig. 2, label:"S7" is an quantized output of fig. 2, num. 21:QIANTIZATION CIRCUIT.) over an information channel ("S7" of figure 2.) to a decoder (Fig. 48, num. 411:DECODING CIRCUIT) for reconstruction of an approximated signal (Fig. 48, num 70 is an output.).

Claims 1, 2, and 3 contain analogous subject matter and are rejected as applied in claim 4, above.

Regarding claim 5, Yamaguchi et al. discloses the method of processing a multi-dimensional signal via multi-scale transform comprising the steps of:

a. Obtaining the multi-dimensional signal (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num. 3:SCREEN-AREA DETERMINING MEANS.)

b. Performing a pattern (A pattern signal from figure 2, label "S2" is used with the output of the transform of fig. 2, num. 17. Note that a human visual characteristics which states that patterns are part of the human visual characteristic in col. 1, lines 18-35 are used in the "assignment" signal "S2" via a weight function of figure 2 in col. 11, lines 1-14 and col. 14, lines 28-31.) adaptive transform (Fig. 2,num. 17 DCT is adaptive because it adapts to changes of the input signal "S1" of figure 2 based on a selector 15 of figure 2.) on the signal (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num. 3:SCREEN-AREA DETERMINING MEANS.) .

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Regarding claim 6, Yamaguchi et al. discloses the method of claim 2 where step b comprises of a combined domain (Fig. 5(a) is the domain.) a pattern (Fig. 5(a), num. 31 shows an outer rectangle pattern.) adaptive transform (Fig. 5(a) is weighted in col. 16, lines 20-31 depending on the human visual characteristics which take patterns in account in col. 11, lines 8-14.).

Claims 7 and 8 were addressed in claim 6.

Regarding claim 9, Yamaguchi et al. discloses the method as in [any one of claim[s] 3[, 5, or 6] where instead of transmitting over an information channel ("S7" of figure 2.) the encoded data (Fig. 2, label:"S7" and another output from quantizer 20 going into figure 2,num. 18 is an quantized output of fig. 2, num. 21:QUANTIZATION CIRCUIT.) is placed onto a storage apparatus (fig. 2,num. 14:REFERENCE MEMORY) or mechanism for the purpose of efficient storage and later decoding.

Regarding claim 10, Yamaguchi et al. discloses the method as in [any one of claims] 3[, 5, or 6] where instead of directly quantizing (fig. 2, num. 21: QUANTIZATION CIRCUIT) the resultant decomposition coefficients (FIG. 2, um. 17 outputs coefficients to fig. 2, num. 21:QUANTIZATION CIRCUIT.) and then encoding (Figure 3, num. 25:ENCODER), the coefficients (FIG. 2, um. 17 outputs coefficients to fig. 2, num. 21:QUANTIZATION CIRCUIT.) are passed through a bit-plane encoder (No quantization is performed on the coefficients in the "dead zone" shown in figure 7(a) and 7(b), numeral 35 in col. 16, lines 34-38 and 55-59 of the quantization circuit 21. Thus the coefficients are passed to encoder 25 of figure 3 without quantization.).

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Regarding claim 11, Yamaguchi et al. discloses the method as in any one of claims 1 or 5 where the multi-dimensional signal (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num. 3:SCREEN-AREA DETERMINING MEANS.) is composed of multiple color ("Color Signal" in col. 1, line 47) or intensity components.

Regarding claim 12, Yamaguchi et al. discloses the method of claim 11 where the signal is 2-D (Signal S1 has an area.) and there are three color components (Color Signal and Luminance Signal in col. 1, line 47.) and these represent Y, U, and V and R,G,B.

Claim 13 was addressed in claim 12.

Regarding claim 14, Yamaguchi et al. discloses the method of claim 11 where the signal is 2-D (Signal S1 has an area.) and there are three color components (Color Signal and Luminance Signal in col. 1, line 47.) and these are any orthogonal color components (The signal S1 is orthogonally transformed in col. 4, lines 50-56.).

Regarding claim 15, Yamaguchi et al. discloses the method as [in any one of claim[s] 2 [or 6] where the multi-dimensional image frame (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num. 3:SCREEN-AREA DETERMINING MEANS.) is a still image frame ("an image" in col. 1, line 16 is used to display the image in col. 1, lines 1-16.)

Regarding claim 16, Yamaguchi et al. discloses the method as in any one of claims 2 or 6 where the multi-dimensional image frame (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num. 3:SCREEN-AREA DETERMINING MEANS.) is an intra-frame ("intraframe" in col. 15, line 4) for a sequence of video images.

Regarding claim 17, Yamaguchi et al. discloses the method as in any one of claims 2 or 6 where the multi-dimensional image frame (Fig. 1, label:"S1" is a multi-dimensional frame with dimensions of an area as shown in figure 1, num. 3:SCREEN-AREA DETERMINING MEANS.) is a residue frame ("S4" is a residue frame based on a subtraction of signals "S1" and "S3" of figure 2.) for a sequence of video images.

Regarding claim 18, Yamaguchi et al. discloses the method as in any one of claims 1 or 6 where the domain adaptive (Fig. 2,num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2,num. 17:DCT contained in fig. 1,num. 10:CODING MEANS) is applied during the calculation of coarser scale representations (Figure 59 shows the DCT transform, 2D DCT FOR BLOCKS (N XN) calculating a coarser or "REDUCED IMAGE" representation.) in [the] a forward transform (Non-inverse transform) of a multi-scale transform (DCT transform).

Regarding claim 19, Yamaguchi et al. discloses the method as in any one of claims 1 or 6 where the domain adaptive (Fig. 2,num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2, num. 17: DCT contained in fig. 1,num. 10: CODING MEANS) is applied during [the] **an** estimation of next finer scale representations (The output of figure 2,num. 18:INVERSE DCT) in [the] **an** inverse transform (Fig. 2,num. 18: INVERSE DCT) of a multi-scale transform during the reconstruction phase (Fig. 2,num. 18: INVERSE DCT is used "to reproduce any signals (col. 15, lines 28-31).") either in conjunction with the or irrespective of the use of the method in claim 18 (The inverse DCT 18 of figure 2 uses the results from DCT 17 of figure 2 as claim in claim 18.).

Regarding claim 20, Yamaguchi et al. discloses the method as in any one of claims 1 or 6 where the domain adaptive (Fig. 2,num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2, num. 17: DCT contained in fig. 1,num. 10: CODING MEANS) is applied in order to construct a sub-band decomposition (Figure 5(a) is a subband decomposition of an image into two regions 31 and 33 in col. 16, lines 39-42.) of a multi-scale transform (DCT transform).

Regarding claim 21, Yamaguchi et al. discloses the method as in any one of claims 18, 19, or 20 where instead of the domain (Fig. 5(a) is an image or domain where a transform takes place.) adaptive (Fig. 2, num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2, num. 17: DCT contained in fig. 1, num. 10: CODING MEANS), the pattern (Fig. 5(a), num. 31 shows an outer rectangle pattern.) adaptive transform (Fig. 5(a) is weighted in col. 16, lines 20-31 depending on the human visual characteristics which take patterns in account in col. 11, lines 8-14.) is used (The DCT transform performs a domain and pattern transform using the human visual characteristics.).

Claim 22 was addressed in claim 21.

Regarding claim 23, Yamaguchi et al. discloses the method as in any one of claims 1 or 6 where the domain (Fig. 5(a) is an image or domain where a transform takes place.) adaptive (Fig. 2, num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2, num. 17: DCT contained in fig. 1, num. 10: CODING MEANS) is applied during the estimation of the next finer level of sub-bands (Fig. 49 shows a series of images with differing resolutions that can be selected.) in a multi-scale transform (Inverse DCT transform) during the reconstruction phase (Fig. 49, label "REPRODUCED SIGNAL" is a reconstructed signal based on the selected image.).

Claim 24 has been addressed in claim 10. The wording is different from both claims 10 and 24, but both are claiming the same function.

Regarding claim 25, Yamaguchi et al. discloses the method as in any one of claims 1 or 6 where the domain (Fig. 5(a) is an image or domain where a transform takes place.) adaptive (Fig. 2, num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2, num. 17: DCT contained in fig. 1, num. 10: CODING MEANS) is applied such that the points external (Fig. 5(a), num. 32 is a rectangular ring that is external to rectangular ring 31.) to the arbitrary domain (Fig. 5(a) shows a rectangular ring 31.) but within the support of [the] a filter (or filters) (Fig. 15, num. 40: SPATIAL-TEMPORAL FILTER has a support of 3 X 3 pixels as shown in figure 10(b).) are excluded (The rectangular ring 31 shown in figure 13(a) has a region excluded or "restrained" for detecting a region 47 as shown in figures 13(b) and 13(c) in col. 17, lines 32-34 and col. 18, lines 34-44.) from [the] a mathematical result (The "restrained" portion of fig. 13(a), num. 31 is outputted to fig. 15, num. 25: ENCODER) of [the] a convolution (Fig. 15, num. 25: ENCODER produces a convolution or mixture of signals that are combined as shown in figure 6.) or weighted average / difference.

Regarding claim 26, Yamaguchi et al. discloses the method as in any one of claims 1 or 6 where the domain (Fig. 5(a) is an image or domain where a transform takes place.) adaptive (Fig. 2,num. 17 DCT is adaptive because it adapts to changes of the input signal based on a selector 15 of figure 2.) transform (fig. 2, num. 17: DCT contained in fig. 1,num. 10: CODING MEANS) is applied such that [the] **a plurality of** points (Figure 5(a) shows another rectangular ring 32.) external to the arbitrary domain (Fig. 5(a) shows a rectangular ring 31.) but within [the] **a support of [the] a filter** (Fig. 10(b) is a filter with a support of 3 X 3.) [(or filters)] **or a plurality of filters** are included in [the] **a mathematical result** (Fig. 9, num. 44 is an adder.) of [the] **a convolution or weighted average / difference** (A difference "1-k" of figure 9, num. 43 is inputted to adder 44.) but are further multiplied (or re-weighted) (Figure 5(a) shows another rectangular ring 32 that is weighted differently from rectangular ring 31 in col. 17, lines 26-29.) by another set of weighting factors ("m and k" in col. 17, lines 26,27).

Regarding claim 27, Yamaguchi et al. discloses the method of claim 26 where the set of additional multiplicative factors ("m and k" in col. 17, lines 26,27) is determined as [the] **a result** (Fig. 8,num. 23: RESOLUTION DETECTING CIRCUIT outputs data.) of calculation of a local measure (Fig. 8, num. 23 measures resolution regions.) characterizing [the] **a transition** (Fig. 8, num. 23 calculates resolution regions that have a transition between regions using respective weights in col. 16, lines 23-26.) at [the] **a boundary of the arbitrary domain** (Fig. 5(a) shows a rectangular ring 31 that has a boundary with another rectangular ring 32.).

Regarding claim 28, Yamaguchi et al. discloses the method of claim 27 where the measure (Fig. 8, num. 23 measures resolution regions.) is based on a statistical function ("weight distribution function" in col. 16, lines 20,21.) of the pixel value differences (The weight distribution function is uses pixels of figure 4, num. 27 or figure 5(a), num. 31 that are weighted differently from another set of pixels of figure 4,num. 29 or fig. 5(a), num. 32 as mentioned in col. 16, lines 1-31.) across the boundary (Fig. 5(a) shows a rectangular ring 31 that has a boundary with another rectangular ring 32.) transition (Fig. 8, num. 23 calculates resolution regions that have a transition between regions using respective weights in col. 16, lines 23-26.).

Regarding claim 29, Yamaguchi et al. discloses the method of claim 28 where the statistical function ("weight distribution function" in col. 16, lines 20,21.) is the mean ("standard deviation" in col. 16, line 6 includes a mean value.).

Regarding claim 30, Yamaguchi et al. discloses the method of claim 28 where the statistical function ("weight distribution function" in col. 16, lines 20,21.) is the median ("normal distribution" in col. 16, line 7 includes a central value.).

Regarding claim 31, Yamaguchi et al. discloses the method of claim 28 where the statistical function ("weight distribution function" in col. 16, lines 20,21.) is based on a weighted average ("normal distribution" in col. 16, line 7 includes a central value.).

Regarding claim 32, Yamaguchi et al. discloses the method of claim 28 where the statistical function ("weight distribution function" in col. 16, lines 20,21.) is based on a weighted average (The weight distribution is based on a standard deviation that inherently contains an average.) with coefficients (or weights) that are nonlinear functions (The standard deviation inherently includes root and power functions.) of the **weighted average** [data values] themselves .

Regarding claim 33, Yamaguchi et al. discloses the method of claim 28 where the statistical function ("weight distribution function" in col. 16, lines 20,21.) is a pre-determined constant (The weight distribution constantly distributes weights in a specified area as mentioned in col. 16, lines 26-31.) .

Regarding claim 34, Yamaguchi et al. discloses the method of claim 26 where the set of additional multiplicative factors ("m and k" in col. 17, lines 26,27) is determined as the result of calculation of a local measure (Fig. 13(b) shows a region 47 or 53 that is measured based on a number of pixels in col. 18, lines 34-46.) characterizing [the] a transition (A region 32 contains a border 47 with region 53 of figure 13(c).) at the boundary of the arbitrary domain (Fig. 5(a) and figure 13(a) show a rectangular ring 31 next to the transition region 32.) and the calculation of the local measure (Fig. 13(b) shows a region 53 that is measured.) is dependent on data (Data from fig. 2,num. 22:INVERSE QUANTIZATION CIRCUIT is provided to INVERSE DCT 18 of figure 2) which is available to [the] a decoder (Fig. 2,num. 18: INVERSE DCT) at the time of [the] an operation when envisioned as part of [the] an inverse transform (Fig. 2, num. 18: INVERSE DCT) or reconstruction phase of a multi-scale transform.

Regarding claim 35, Yamaguchi et al. discloses the method of claim 34 where the calculation of the local measure (Fig. 13(b) shows a region 47 or 53 that is measured based on a number of pixels in col. 18, lines 34-46.) is based on one or more coarser scales of representation (Fig. 49 shows a series of the signal S1 that has a progression of coarseness.) of the signal (A signal S1 of figure 1 has a domain of 16 X 16 pixels in col. 14, lines 59-61.) which have already been decoded (Fig. 2, num. 22: INVERSE QUANTIZATION CIRCUIT outputs a decoded signal to figure 18: INVERSE DCT.) and thus made known to the decoder (Fig. 2, num. 22: INVERSE QUANTIZATION CIRCUIT) by the time of the inverse transform step (Fig. 2, num. 18: INVERSE DCT.).

Regarding claim 36, Yamaguchi et al. discloses the method of claim 34 where the calculation of the local measure (Fig. 13(b) shows a region 47 or 53 that is measured based on a number of pixels in col. 18, lines 34-46.) is based on a motion compensated (Fig. 2, num. 11: MOTION-VECTOR DETECTION CIRCUIT) model frame (or equivalent)(Fig. 2, num. 14: REFERENCE FRAME MEMORY is inputted to figure 2, num. 11 that performs motion compensation.) that has already been decoded (via output arrow of fig. 2, num. 22: INVERSE QUANTIZATION) and thus made known to the decoder (Fig. 2, num. 22: INVERSE QUANTIZATION CIRCUIT) by the time of the inverse transform step (Fig. 2, num. 18: INVERSE DCT) in the context of an encoder-decoder system (Fig. 2, num. 10) related to the efficient transmission (Three outputs of figure 2, num. 10.) or storage of a sequence of video data.

Regarding claim 37, Yamaguchi et al. discloses the method as in any one of claims 25 or 26 where [the] a needed function for renormalization, i.e. replacement of [the] **a plurality of** missing filter coefficients (Fig. 37, num. 500:AVERAGE VALUE SEPARATING CIRCUIT performs a function of assigning coefficient values of zero as shown in figure 38.), is accomplished by a statistical function (Fig. 37, num. 500 AVERAGE VALUE) of [the] **a plurality of** remaining pixel values (Fig. 38 shows remaining pixels values as white squares in the left array of pixels.) which are located at points contained within the arbitrary shaped domain (Fig. 5(a) and figure 13(a) show a rectangular ring 31 next to the transition region 32 that corresponds to an input signal of figure 37,num. 10:IMAGE SIGNAL. Thus, the array of pixels in figure 38 that correspond to the rectangular rings 31 and 32 are from the signal of figure 37, num .10:IMAGE SIGNAL.).

Claim 38 was addressed in claim 29.

Claim 39 was addressed in claim 30.

Claim 40 was addressed in claim 31.

Claim 41 was addressed in claim 32.

Regarding claim 42, Yamaguchi et al. discloses the method of claim 37 where some form of outlier rejection ("restrain" in col. 17, line 34) is used to ensure that outliers ("first region 31 of figure 5(a)" in col. 17, lines 27,28.) remaining inside the intersection of the domain (The image of fig. 5(a).) and the filter support (Fig. 10(b) shows a filter with a support of 3 X 3 that scans the region of the image in fig. 5(a).) do not disrupt the local accuracy or efficiency (Using figure 8, the "filter" 40 "restrains" any "codes" in col.

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17, lines 32-35 produced for the DCT transform of fig. 2,num. 17 or encoder 25 of fig.

8.) of the transform (fig. 2, num. 17: DCT contained in fig. 1,num. 10: CODING MEANS).

### ***Conclusion***

9. The prior art made of record and not relied upon is considered pertinent to applicant's disclosure.

Cho et al. (US Patent 6,501,861 B1) is pertinent as teaching a method of transforming images using shapes as shown in figure 7.

Sathe et al. (US Patent 5,909,249 A) is pertinent as teaching a method of using a transform with non-linear characteristics shown in figs. 3-5.

Quenouille, Introductory Statistics, Pergamon Press Ltd.,

pp. 6,7, ©1966, is pertinent as teaching a method of standard deviation that includes a mean and average. This reference is applicable to claims 29 and 31.

10. Any inquiry concerning this communication or earlier communications from the examiner should be directed to Dennis Rosario-Vasquez whose telephone number is 703-305-5431. The examiner can normally be reached on 9-5.

If attempts to reach the examiner by telephone are unsuccessful, the examiner's supervisor, Leo Boudreau can be reached on 703-305-4706. The fax phone number for the organization where this application or proceeding is assigned is 703-872-9306.

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Dennis Rosario-Vasquez  
Unit 2621

  
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Application Number	10/032,394
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<b>Filing Date</b>	<b>December 19, 2001</b>
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First Named Inventor	Adityo Prakash
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Group Art Unit	2613
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<b>Examiner Name</b>	not yet known
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<b>Attorney Docket Number</b>	<b>10006.000610</b>
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**U.S. PATENT DOCUMENTS**

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## FOREIGN PATENT DOCUMENTS

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		Filing Date	December 19, 2001
		First Named Inventor	Adityo Prakash
		Group Art Unit	2613
		Examiner Name	not yet known
		Attorney Docket Number	10006.000610
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DJW	V	FARUK M.O. ERYURLU, et al. "Very Low Bit-Rate Segmentation-based Video Coding"; pgs. 151-154, XP-000964709; University of Surrey, Guildford, United Kingdom.	
DJW	W	YURAO FENG, et al. "Adaptive Object Tracking and Video Compression with Dynamic Contours"; total pgs.:11; XP-002112425; Fifteenth National Radio Science Conference February 24-26, 1998, Helwan, Cairo, Egypt.	
DJW	X	JONG-LAK KIM, et al., "Daewoo Proposal For Object Scalability"; pgs. 1-9; XP-000994686; International Organization For Standardization Organization Interanationale De Normalisation ISO/IEC JTC1/SC29/WG11 Coding Of Moving Pictures And Associated Audio; January 1993, Munich, Germany.	

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<b>Filing Date</b>	December 19, 2001
<b>First Named Inventor</b>	Adityo Prakash
<b>Group Art Unit</b>	2613
<b>Examiner Name</b>	not yet known
<b>Attorney Docket Number</b>	10006.000610

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Sheet	1	of	2
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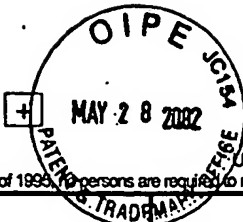
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Application Number	10/032,394
Filing Date	December 19, 2001
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### OTHER PRIOR ART - NON PATENT LITERATURE DOCUMENTS

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DPW	C	PETER J. BURT, et al., The Laplacian Pyramid as a Compact Image Code; April 1983, pgs. 532-540, Vol. COM-31; IEEE Transactions on Communications.	
DPW	D	AMIR SAID, et al., A New, Fast, and Efficient Image Codec Based on Set Partitioning in Hierarchical Trees; June 1996, pgs. 243-250, Vol. 6 No. 3; IEEE Transactions on Circuits and Systems for Video Technology.	
DPW	E	MICHAEL W. MARCELLIN, et al., Trellis Coded Quantization of Memoryless and Gauss-Markov Sources; January 1990, pgs. 82-93, Vol. 38 No.1; IEEE Transactions on Communications.	
DPW	F	JEROME M. SHAPIRO, An Embedded Hierarchical Image Coder Using Zerotrees Of Wavelet Coefficients; pgs. January 1993, pgs. 214-223 The David Sarnoff Research Center, Princeton, N.J.	
DPW	G	THOMAS SIKORA, et al., Express Letters; June 1995, pgs. 254-258, Vol. 5 No. 3; IEEE Transactions on Circuits and Systems for Video Technology.	
DPW	H	ANDRE KAUP, Object-Based Texture Coding of Moving Video in MPEG-4; February 1999, pgs.5-15, Vol. 9 No. 1; IEEE Transactions on Circuits and Systems for Video Technology.	
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	N	MARK DE BERG, et al.; Computational Geometry, Algorithms and Applications; Department of Computer Science, Utrecht University, The Netherlands; Pohang University of Science and Technology, South Korea.	

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**Notice of References Cited**

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2621

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**U.S. PATENT DOCUMENTS**

*		Document Number Country Code-Number-Kind Code	Date MM-YYYY	Name	Classification
	A	US-6,501,861 B1	12-2002	Cho et al.	382/243
	B	US-5,978,514 A	11-1999	Yamaguchi et al.	382/243
	C	US-5,909,249 A	06-1999	Sathe et al.	375/240.18
	D	US-			
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**FOREIGN PATENT DOCUMENTS**

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	N					
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	S					
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**NON-PATENT DOCUMENTS**

*		Include as applicable: Author, Title Date, Publisher, Edition or Volume, Pertinent Pages)
	U	Quenouille, M. H., Introductory Statistics, 1966, Pergamon Press Ltd., pp. 6-7
	V	
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\*A copy of this reference is not being furnished with this Office action. (See MPEP § 707.05(a).)  
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# INTRODUCTORY STATISTICS

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the set of ten observations 104, 107, 111, 112, 114, 115, 117, 119, 124, 127, has an arithmetic mean of 115, and the differences or deviations from the mean, irrespective of sign, are 11, 8, 4, 3, 1, 0, 2, 4, 9, 12, so that the mean deviation is

$$[11+8+4+3+1+0+2+4+9+12]/10=5.4$$

Mathematically, the differences are denoted by  $x_1 - \bar{x}$ ,  $x_2 - \bar{x}$ ,  $x_3 - \bar{x}$  . . . and the disregard for the sign is expressed by parallels thus

$$|x_1 - \bar{x}|, |x_2 - \bar{x}|, |x_3 - \bar{x}|, \dots$$

so that the mean deviation is

$$\frac{|x_1 - \bar{x}| + |x_2 - \bar{x}| + |x_3 - \bar{x}| + \dots + |x_n - \bar{x}|}{n} = \frac{\sum |x - \bar{x}|}{n}$$

This measure of spread will not be affected by a few large or small observations in the same manner as the range. It can also be used for comparative purposes since it is virtually independent of the number of observations taken. (It is not completely independent of the number of observations, but provided the number of observations exceeds ten it is effectively so.) The magnitude of the mean deviation will indicate the region within which slightly more than half the observations will fall. In the above example slightly more than half the observations are within 5.4 of the mean 115 *i.e.* between 109.6 and 120.4.

To demonstrate the use of the range and mean deviation, suppose that 92, 99, 104, 110, 113, 115, 118, 121, 125 and 133 is a second set of ten observations. The arithmetic mean of this set of observations is 113 and the deviations from the mean, ignoring the signs, are 21, 14, 9, 3, 0, 2, 5, 8, 12 and 20, so that the mean deviation is

$$[21+14+9+3+0+2+5+8+12+20]/10=9.4$$

Here, slightly more than half the observations lie between  $113-9.4$  and  $113+9.4$  *i.e.* 103.6 and 122.4. The spreads or scatters of the measurements in the two sets of observations are thus in the ratio  $9.4/5.4=1.74$ , and scatter in the second set is 1.74 times that in the first. A comparison of the scatter in the two sets of observations using the range gives the ratio  $\frac{133-92}{127-104} = \frac{41}{23} = 1.78$ , which agrees remarkably well with this value.

**1.8 Measures of spread: standard deviation and variance**—The standard deviation is the most commonly used measure of spread and its square, which is called the variance, occurs almost as frequently. The variance is defined to be the average of the squared deviations of each observation from the arithmetic mean, or briefly, the mean squared deviation. Thus for the

112, 114, 115, 117, 119, 124, 127, differences or deviations from the mean are 1, 0, 2, 4, 9, 12, so that the mean

$$[1 + 0 + 2 + 4 + 9 + 12]/10 = 5.4$$

noted by  $x_1 - \bar{x}$ ,  $x_2 - \bar{x}$ ,  $x_3 - \bar{x}$  . . . .  
 noted by parallels thus

$$|x_3 - \bar{x}|, \dots$$

$$\dots + |x_n - \bar{x}| = \frac{\sum |x - \bar{x}|}{n}$$

affected by a few large or small observations. It can also be used for a set of observations which is nearly independent of the number of observations exceeds ten it is the mean deviation will indicate the number of observations which will fall. In a half the observations are within 10 and 120.4.

and mean deviation, suppose that 125 and 133 is a second set of ten observations this set of observations is 113 and the signs, are 21, 14, 9, 3, 0, 2, 5, on is

$$[21 + 14 + 9 + 3 + 0 + 2 + 5 + 8 + 12 + 20]/10 = 9.4$$

observations lie between 113-9.4 and 133+9.4. The range of the measurements is 20 but in the ratio  $9.4/5.4 = 1.74$ , and is less than that in the first. A comparison of the two sets of observations using the range gives the ratio 1.78 which agrees remarkably well with this value.

**Deviation and variance**—The standard deviation is a measure of spread and its square, the variance, is almost as frequently used. The variance is the sum of the squared deviations of each observation from the mean squared deviation. Thus for the

first set of observations given on p 6 the deviations are - 11, - 8, - 4, - 3, - 1, 0, 2, 4, 9 and 12, and the variance is

$$[121 + 64 + 16 + 9 + 1 + 0 + 4 + 16 + 81 + 144]/10 = 45.6$$

The standard deviation or root mean squared deviation is thus  $\sqrt{45.6} = 6.75$ .

Under this definition the standard deviation and variance will not be much affected by a few large or small observations. For the purposes of comparison they will not be greatly influenced by the numbers of observations in each group although, if the number of observations tends to be small, the standard deviation and variance tend to be reduced\*. This difficulty is overcome by altering the definition slightly, so that the variance is taken as *the total of the squared deviations divided by one less than the number of observations*†. Thus, in the above example, the variance by the revised definition is

$$[121 + 64 + 16 + 9 + 1 + 0 + 4 + 16 + 81 + 144]/9 = 50.67$$

and the standard deviation is  $\sqrt{50.67} = 7.12$ . It is impossible to justify completely the use of one less than the number of observations in calculating the mean squared deviation or variance without recourse to mathematics and, for this reason, a fuller mathematical justification is given on p 51. Since the deviations of the observations from the mean can be represented by  $x_1 - \bar{x}$ ,  $x_2 - \bar{x}$ ,  $x_3 - \bar{x}$ , . . .  $x_n - \bar{x}$ , the definition of variance or mean squared deviation is

$$\frac{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + (x_3 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}{n - 1} = \frac{\sum (x - \bar{x})^2}{n - 1}$$

and the standard deviation is  $\left( \frac{\sum (x - \bar{x})^2}{n - 1} \right)^{\frac{1}{2}}$ .

If the second set of observations on p 6 is used, its variance is found to be

$$[441 + 196 + 81 + 9 + 0 + 4 + 25 + 64 + 144 + 400]/9 = 151.56$$

and its standard deviation is  $\sqrt{151.56} = 12.31$ . Thus, the ratio of the standard deviations of the two sets of observations is  $12.31/7.12 = 1.73$ , which agrees with the values of 1.74 and 1.78 which were derived using the mean deviation and range.

It is usually true to say that about two thirds of any set of observations differ from the mean by less than the standard deviation. For the first set of ten observations roughly two thirds of the observations lie between  $113 \pm 7.12$  and  $115 \pm 7.12$  i.e. between 107.88 and 122.12, while for the

\* If only one observation is taken, the standard deviation by this definition would be zero, whereas it is really impossible to get any information concerning scatter from only one observation.

† Under this definition, when only one observation is taken, the standard deviation is now 0/0, an indeterminate quantity.